## ESTIMATION OF PALAY PRODUCTION WITH THE 1960 AGRICULTURAL CENSUS AS THE SAMPLING FRAME\*

Bv

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Sample surveys must be designed to provide current statistics about the country's agricultural development. the most important uses of agricultural census results is to serve as a framework for current agricultural statistics (1). In general, data from the agricultural censuses are obtained by enumeration or by the use of a high sampling fraction of the farm households. Thus, the results of the agricultural census can be used as the framework of the agricultural sample survevs.

This paper will illustrate some of the approaches to this problem of designing sample surveys with the agricultural agricultural census as the sampling frame. The results of the Philippine Agricultural Census of 1960 will be used in the estimation of palay production in the five selected provinces of Abra, Bulacan, Pampanga, Tarlac, and Zambales.

## I. Palay Production

The Philippine 1960 Agricultural Census (2) contains data on palay production in cavans of 44 kilograms by municipality. The production data are given under five categories or strata. namely: (a) First crop, irrigated; (b) first crop, not irrigated; (c) second crop, irrigated; (d) second crop, not irrigated; and (e) kaingin and upland. In addition to palay production, the total number of farms reporting and total hectarage under palay also are tabulated by each type of strata. We will show how these two concomitant variables can be used to estimate palay production by province.

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### II. Comparison of Efficiency of Estimators

Five different estimators of palay production will be used and their efficiencies will be compared (3,4,5). These estimators of total palay production of the province are as follows:

Simple random (X-only) 
$$= \overline{T}_x = N\overline{x};$$
Stratified (optimum)  $= \overline{T}_y(oa) = N\overline{x}(oa);$ 
Ratio of means  $= \overline{T}_q = \overline{q}Z \text{ or } = \overline{q}Y;$ 
Separate ratio (st)  $= \overline{T}_q(st) = \sum_{i=1}^L \overline{q}_i Z_i$ 
or  $\sum_{i=1}^L \overline{q}_i Y_i;$ 
Combined ratio (st)  $= \overline{T}_c(st) = q(st)Z$ 
or  $= q(st)Y;$ 
and the
Unbiased separate ratio  $= \overline{T}_u$ .

The variances of each of these estimators are given in Table 1. The variance of  $\mathbf{T}_{\mathbf{X}}$  is

$$N(N-n) S^2(X_{ij})/n$$

and this variance is not given in the table. For the ratio estimators, the number of farms reporting and the hectarage under the palay crop are used as concomitant variables. The statistics on palay production  $(X_{ij})$ , number of farms reporting  $(Z_{ij})$  and hectarage  $(Y_{ij})$  for the provinces of Abra, Bulacan, Pampanga, Tarlac, and Zambales are shown in Tables 2a, 2b, 2c, 2d and 2e, respectively, where

N is the province or universe size,

N, is the stratum size (i=1, 2, ..., 5),

n is the sample size for the province,

n, is the sample size for the stratum,

X, Z, or Y is the total for the province,

X, Z, or Y, is the total for the ith stratum,

TABLE 1
SUMMARY OF DIFFERENT ESTIMATORS OF POPULATION TOTAL, X,\* THEIR VARIANCES AND ESTIMATES OF VARIANCE IN STRATIFIED SAMPLING.

| Type of estimator                      | Form of estimators   | Variance   | Estimate of variance  |
|--|--|--|---|
| Stratified                             | $T(st) = N\overline{x}(st)$ $= \sum_{i=1}^{L} N_{i}\overline{x}_{i}$                                       | $\sum_{i=1}^{L} N_{i} (N_{i} - n_{i}) S_{i}^{2} (X_{ij}) / n_{i}$  | $s^{2}\left[\bar{T}(st)\right] = \sum_{i=1}^{L} N_{i}(N_{i}-n_{i}) s_{i}^{2}(X_{ij})/n_{i}$   |
| Ratio of means                         | i<br>T = qZ or = qT  | $(N-n)N \left[ s^2(x_{ij}) + q^2 s^2(z_{ij}) - 2qs(x_{ij}, z_{ij}) \right] /n$   | $(N-n) N \left[ s^{2}(X_{ij}) + q^{2} s^{2}(Z_{ij}) -2qs(X_{ij}, Z_{ij}) \right] /n$  |
| Separate ratio of means                | $T_{Q}(st) = \sum_{i=1}^{L} \bar{q}_{i}Z_{1}$  | $\sum_{i=1}^{L} N_{i} (N_{i} - n_{i}) \left[ s_{i}^{2} (X_{ij}) + Q_{i}^{2} s_{i}^{2} (Z_{ij}) -2Q_{i} s_{i} (X_{ij}, Z_{ij}) \right] / n_{i}$ | $s^{2}\left[\tilde{T}_{Q}(st)^{2}\right]\sum_{i=1}^{L}\tilde{N}_{i}(\tilde{N}_{i}-n_{i})\left[s_{i}^{2}(\tilde{X}_{ij})+\bar{q}_{i}^{2}s_{i}^{2}(\tilde{Z}_{ij})-2\bar{q}_{i}s(\tilde{X}_{ij},\tilde{Z}_{ij})\right]/n$ |
| Combined ratio of meuns                | $\tilde{T}_{C}(st) = \begin{bmatrix} \bar{x}(st)/\dot{z}(st) \end{bmatrix} Z$                              | $\sum_{i=1}^{L} N_{i} (N_{i}^{-n}_{i}) \left[ s_{i}^{2} (X_{ij}) + Q^{2} s_{i}^{2} (Z_{ij}) -2 Q s_{i} (X_{ij}, Z_{ij}) \right] / n_{i}$       | $s^{2} \left[ \tilde{T}_{C}(st) \right] = \sum_{i=1}^{L} N_{i} (N_{i} - n_{i}) \left[ s_{i}^{2} (X_{ij}) + q^{2} s_{i}^{2} (Z_{ij}) - 2q s_{i} (X_{ij}, Z_{ij}) \right] / n$  |
| Separate<br>unbiased ratio<br>of means | $\tilde{T}_{u}(st) = \sum_{i=1}^{L} \left\{ \bar{r}_{i} Z_{i} + \left[ (N_{i} - 1) r_{i} \right] \right\}$ | Use variance for separate  | Use estimator $s^2 \left[ \tilde{T}_{Q}(st) \right]$  |
| •                                      |  | ratio $\sigma^2 \left[ \tilde{\tau}_{\mathbf{Q}}(\mathbf{st}) \right]$   |   |

\*If we want to estimate the population mean  $\bar{X}$ , then we divide the estimators of total by N and the corresponding variance by  $N^2$ 

| Parameters<br>of stratum         |             | s          | trata      |           |           | Parameters of province          |
|----------------------------------|-------------|------------|------------|-----------|-----------|---------------------------------|
|                                  | (a)         | (b)        | (c)        | (d)       | (e)       |                                 |
| N,                               | 25          | 22         | 23         | 17        | 24        | N = 111                         |
| n (oa)                           | 10          | 5          | 5          | 1         | 2         | n = 23                          |
| $(N_i - n_i)$                    | 15          | 17         | 18         | 16        | 22        |                                 |
| $X_{i}$                          | 234,996     | 150,423    | 85,634     | 11,440    | 31,069    | X = 513,562                     |
|                                  | 6,715       | 9,353      | 2,949      | 929       | 2,614     | Z = 22,560                      |
| Z <sub>i</sub><br>Y <sub>i</sub> | 8,392       | 8,651      | 2,915      | 758       | 2,447     | Y = 23,162                      |
| $S_i^2(Z_{ij})$                  | 110,684,260 | 31,237,410 | 31,114,311 | 1,093,155 | 6,405,335 | $S^2(X_{ij}) = 48,998,431$      |
| $S_i^2(Y_{ij})$                  | 32,425      | 102,561    | 23,675     | 8,599     | 10,457    | $S^2(Z_{ij}) = 52,176$          |
| $S_i^2(X_{ij})$                  | 141,663     | 105,443    | 34,928     | 4,849     | 24,911    | $S^2(Y_{ij}) = 82,467$          |
| $S(X_{ij},Z_{ij})$               | 1,478,676   | 1,548,374  | 705,595    | 82,595    | 151,786   | $S(X_{ii},Z_{ii}) = 1,144,993$  |
| $S_i(X_{ij}Y_{ij})$              | 3,600,899   | 1,706,042  | 947,901    | 64,977    | 105,763   | $S(X_{ij}, Y_{ij}) = 1,745,204$ |
| $Q(X_{z}/Z)$                     | 35.00       | 16.08      | 29.04      | 12.31     | 11.89     | Q(X/Z) = 22.76                  |
| $Q_i(X_i/Y_i)$                   | 28.00       | 17.39      | 29.11      | 15.10     | 12.70     | Q(X/Y) = 22.17                  |

<sup>\*</sup>A cavan of palay weighs 44 kilograms.

TABLE 2b

PARAMETERS OF PALAY PRODUCTION (X<sub>ij</sub>) IN CAVANS,\*

NUMBER OF FARMS REPORTING (Z<sub>ij</sub>), AND HECTARAGE (Y<sub>ij</sub>).

BULACAN PROVINCE. JULY 1959 TO JUNE 1960.

| Parameters of stratum |               | S             | Strata         |             |               | Parameters of Province                |  |  |
|-----------------------|---------------|---------------|----------------|-------------|---------------|---------------------------------------|--|--|
|                       | (a)           | (b)           | (c)            | (d)         | (e)           |                                       |  |  |
| N,                    | 19            | 24            | 20             | 12          | 16            | N = 91                                |  |  |
| n <sub>i</sub> (oa)   | 5             | 7             | 3              | 2           | 1             | n = 18                                |  |  |
| $(N_i - n_i)$         | 14            | 17            | 17             | 10          | 15            |                                       |  |  |
| Χ,                    | 822,977       | 1,041,602     | 277,687        | 77,312      | 88,429        | X = 2,308,007                         |  |  |
| $\mathbf{Z_{i}}^{i}$  | 10,483        | 18,380        | <b>4,62</b> 3  | 1,273       | 1,890         | Z = 36,649                            |  |  |
| $\mathbf{Y}_{i}^{'}$  | 19,894        | 33,926        | <b>8,34</b> 3  | 3,853       | 3 <b>,715</b> | Y = 67,731                            |  |  |
| $S_i^2(X_{ij})$       | 1,686,133,700 | 2,456,576,552 | 578,428,219    | 457,443,324 | 89,998,872    | $S^2(X_{ij}) = 1,459,790,95$          |  |  |
| $S_i^2(Z_{i})$        | 215,103       | 668,084       | 133,783        | 175,471     | 30,672        | $S^2(Z_{ij}) = 333,74$                |  |  |
| $S_i^2(Y_{ij})$       | 924,192       | 2,850,606     | 503,056        | 248,570     | 170,858       | $S^2(Y_{ij}) = 1,333,98$              |  |  |
| $S_i(X_{ii},Z_{ii})$  | 18,267,436    | 39,436,315    | 8,647,926      | 7,267,317   | 1,552,170     | $S(X_{ij},Z_{ij}) = 21,151,54$        |  |  |
| $S_i(X_{ij},Y_{ij})$  | 39,146,502    | 82,300,869    | 16,996,456     | 10,663,103  | 3,853,838     | $S(X_{ij}^{3}Y_{ij}^{3}) = 42,890,38$ |  |  |
| $Q_i(X_i/Z_i)$        | 78.50         | 56.67         | . 60.07        | 60.73       | . 46.79       | (QX/Z) = 62.98                        |  |  |
| $Q_i(X_i/Y_i)$        | 41.36         | 30.70         | 3 <b>3.7</b> 8 | 41.73       | 23.80         | Q(X/Y) = 34.08                        |  |  |

<sup>\*</sup>A cavan of palay weighs 44 kilograms.

| Parameters of stratum        |               | S             | trata       |            |            | Parameters of province          |
|------------------------------|---------------|---------------|-------------|------------|------------|---------------------------------|
|                              | (a)           | (b)           | . (c)       | (d)        | (e)        | province                        |
| N,                           | 21            | 21            | 17          | 16         | 9          | N = 84                          |
| n <sub>i</sub> (oa)          | 10            | 9             | 4           | 1          | 1          | n = 25                          |
| $(N_i - n_i)$                | 11            | 12            | 13          | 15         | 8          |                                 |
| $X_{i}$                      | 1,220,455     | 809,399       | 483,899     | 31,303     | 45,088     | X = 2,590,144                   |
| $\mathbf{Z}_{i}$             | 11,804        | 9,410         | 6,568       | 505        | 1,024      | Z = 29,311                      |
| $\mathbf{Z}_{_{\mathbf{i}}}$ | 32,124        | 24,251        | 14,308      | 1,107      | 1,803      | Y = 73,593                      |
| $S^2(X_{\cdot;})$            | 2,091,118,610 | 1,980,008,430 | 554,418,083 | 20,053,831 | 38,281,873 | $S^2(X_{i}) = 1,524,387,116$    |
| $S^2(Z_{:;})$                | 147,870       | 219,154       | 92,726      | 3,850      | 15,649     | $S^2(Z_{ij}) = 148,20$          |
| $S_i^2(Y_{ij})$              | 1,345,595     | 1,461,167     | 566,536     | 24,190     | 57,903     | $S^2(Y_{ij}) = 1,098,54$        |
| $S(X_{\cdot,\cdot},Z_{ii})$  | 16,749,156    | 19,687,977    | 6,780,676   | 276,270    | 762,741    | $S(X_{ij},Z_{ij}) = 14,282,49$  |
| $S(X_{ij}, Y_{ij})$          | 51,300,078    | 53,138,905    | 17,358,867  | 696,219    | 1,454,939  | $S(X_{ij}, Y_{ij}) = 40,234,76$ |
| $Q(X_{i}/Z_{i})$             | 103.39        | 86.02         | 73.68       | 61.99      | 44.03      | Q(X/Z) = 88.37                  |
| Q(X, Y)                      | 37.99         | 33.38         | 33.82       | 28.27      | 25.01      | Q(X/Y) = 35.20                  |

<sup>\*</sup>A cavan of palay weighs 44 kilograms.

PARAMETERS OF PALAY PRODUCTION  $(X_{ij})$  IN CAVANS,\* NUMBER OF FARMS REPORTING  $(Z_{ij})$ , AND HECTARAGE  $(Y_{ij})$  TARLAC PROVINCE. JULY 1959 TO JUNE 1960.

TABLE 2d

| Parameters of stratum        |                | S              | trata          |           |             | Parameters of province            |
|------------------------------|----------------|----------------|----------------|-----------|-------------|-----------------------------------|
|                              | (a)            | (b)            | <b>(</b> c)    | (d)       | (e)         |                                   |
| $N_{i}$                      | 16             | 17             | 13             | 14        | 14          | N = 74                            |
| n <sub>i</sub> (oa)          | 9              | 4              | 1              | 1         | 1           | n <u>==</u> 15                    |
| $(N_i - n_i)$                | 7              | 13             | 12             | 13        | 13          |                                   |
| X                            | 1,367,773      | 1,520,281      | 192,424        | 20,593    | 173,940     | X = 3,275,011                     |
| $Z_{i}$                      | 10,688         | 23,295         | 2,185          | 304       | 4,011       | Z = 40,483                        |
| $\mathbf{Y}_{\mathbf{i}}$    | 31,209         | 51,446         | 5,791          | 743       | 7,926       | Y = 97,115                        |
| $S^2(X_{ij})$                | 27,849,077,307 | 4,427,164,823  | 409,984,984    | 5,311,576 | 417,623,094 | $S^2(X_{ij}) = 7,013,288,273$     |
| $S_i^2(\mathbf{Z}_{ij})$     | 711,458        | 918,636        | 42,526         | 860       | 94,247      | $S^2(Z_{ij}) = 628,467$           |
| $S_i^2(Y_{ij})$              | 9,221,042      | 4,206,125      | 344,710        | 6,899     | 882,208     | $S^2(Y_{ij}) = 4,459,278$         |
| $S_i(X_{ii},Z_{ii})$         | 105,206,436    | 57,089,377     | 3,956,044      | 57,495    | 5,876,112   | $S(X_{ij},Z_{ij}) = 53,479,605$   |
| $S(X_{ij}^{ij},Y_{ij}^{ij})$ | 440,883,478    | 134,385,721    | 11,498,142     | 190,571   | 19,093,511  | $S(X_{ij}, Y_{ij}) = 168,603,753$ |
| $Q(X_i/Z_i)$                 | 127.97         | 65.26          | 88.06          | 67.74     | 43.36       | Q(X/Z) = 80.89                    |
| $Q(X_i/Y_i)$                 | 43.82          | <b>29.55</b> . | 3 <b>3.2</b> 2 | 27.71     | 21,94       | Q(X/Y) = 33.72                    |

<sup>\*</sup>A cavan of palay weighs 44 kilograms.

TABLE 2e

PARAMETERS OF PALAY PRODUCTION (X<sub>ij</sub>) IN CAVANS,\*

NUMBER OF FARMS REPORTING (Z<sub>ij</sub>), AND HECTARAGE (Y<sub>ij</sub>).

ZAMBALES PROVINCE. JULY 1959 TO JUNE 1960.

| Parameters of stratum          |             |             | Strata  |         |           | province<br>Parameters of       |
|--------------------------------|-------------|-------------|---------|---------|-----------|---------------------------------|
|                                | (a)         | (b)_        | (c)     | (d)     | (e)       |                                 |
| N <sub>i</sub>                 | 14          | 14          | 9       | 6       | 13        | N = 56                          |
| n (oa)                         | 4           | 4           | 1       | 1       | 1         | n = 11                          |
| $(N_i - n_i)$                  | 10          | 10          | 8       | 5       | 12        |                                 |
| $\mathbf{X}_{\mathbf{i}}$      | 163,491     | 434,836     | 5,087   | 3,796   | 17,704    | X = 624,914                     |
| Z.                             | 2,636       | 9,101       | 120     | 103     | 874       | Z = 12,082                      |
| Y <sub>i</sub>                 | 4,462       | 13,894      | 190     | 122     | 1,158     | Y = 19,826                      |
| $S^2(X)$                       | 318,894,387 | 251,224,571 | 777,501 | 559,091 | 3,396,198 | $S^2(X_{ij}) = 289,671,845$     |
| $S^2(\mathbf{Z}_{\cdot\cdot})$ | 76,047      | 119,868     | 430     | 225     | 8,137     |                                 |
| $S_i^2(Y_{ij})$                | 236,588     | 352,143     | 1,020   | 327     | 16,102    | $S^2(Y_{ij}) = 293,773$         |
| $S(X_{.,},Z_{.,})$             | 4,900,321   | 5,127,630   | 18,118  | 10,993  | 159,680   | $S(X_{ij},Z_{ij}) = 5,680,636$  |
| $S_i(X_{ij},Y_{ij})$           | 8,640,417   | 8,727,399   | 26,678  | 12,510  | 219,422   | $S(X_{ij}, Y_{ij}) = 8,960,977$ |
| $Q(X_{i}/Z_{i})$               | 62.02       | 46.68       | 42.39   | 36.85   | 20.26     | Q(X/Z) = 52.72                  |
| $Q_i(X_i^{'}/Y_i)$             | 36.64       | 31.30       | 26.77   | 31.11   | 15.29     | Q(X/Y) = 31.52                  |

<sup>\*</sup>A cavan of palay weighs 44 kilograms.

 $S^{2}(X_{ij})$ ,  $S^{2}(Z_{ij})$ , or  $S^{2}(Y_{ij})$ is the variance for the province,

$$S^2(X_{ij})$$
,  $S^2(Z_{ij})$ , or  $S^2(Y_{ij})$   
is the variance for the i<sup>th</sup> stratum,

Q(X/Z) or Q(X/Y) is the ratio for the province,

and

$$Q_i(X_i/Z_i)$$
 or  $Q_i(X_i/Y_i)$  is the ratio for the i<sup>th</sup> stratum.

Note that N, the province or universe size, is assumed to be independent of Z, the total number of farms reporting.

These statistics are used to derive the variances of the estimators for a given province. These variances are compared and the relative efficiencies (R.E.) are derived. The results for a 20 percent sample of municipalities are given in Tables 3a, 3b, 3c, 3d, and 3e for the provinces of Abra, Bulacan, Pampanga, Tarlac, and Zambales, respectively.

The results indicate that the group of ratio estimators is superior to either the simple random or stratified (optimum) estimator. In turn, the separate ratio estimator  $[\widetilde{T}_q(st)]$  is more efficient than the ratio means  $[\widetilde{T}_q]$  or the combined ratio  $[\widetilde{T}_c(st)]$  estimator. With number of farms  $(Z_{ij})$  as the concomitant variable the R.E. of  $\widetilde{T}_q(st)$  to  $T_x$  ranges from 426 percent for Abra (Table 3a) to 4742 percent from Zambales (Table 3e). With hectarage  $(Y_{ij})$  as the additional variable, the R.E. ranges from 682 percent for Abra (Table 3a) to 6669 percent for Bulacan (Table 3b). The  $cv \mid \widetilde{T}_x \mid$  for Pampanga was 24 percent. When we use the separate ratio estimator  $[\widetilde{T}_q(st)]$ , the cv was 3 percent, indicating considerable gain of statistical precision in the use of  $\widetilde{T}_q(st)$  over  $\widetilde{T}_x$ . The variance of  $\widetilde{T}_q(st)$  is not given as it is assumed to be equal to that of  $\widetilde{T}_q(st)$ .  $\overline{T}_u(st)$  may be used to remove the bias in  $\widetilde{T}_q(st)$ .

Table 3a

VARIANCE OF ESTIMATOR AND RELATIVE EFFICIENCY OF ESTIMATES
FOR PALAY PRODUCTION.
ABRA PROVINCE. JULY 1959 TO JUNE 1960

|  |                       |          | Concomita | nt variable           |        |      |  |
|--|-----------------------|----------|-----------|-----------------------|--------|------|--|
|  |                       | Number o |           | Hectarage             |        |      |  |
| Type of estimator                                  | Variance<br>(000,000) | R.E.%*   | cv %      | Variance<br>(000,000) | R.E.%* | cv % |  |
| Simple random $= \overline{T}_x$ (X-only)          | 20,809                | 100      | 28        | 20,809                | 100    | 28   |  |
| Stratified (optimum) $\equiv \overline{T}_{X}(oa)$ | 12,435                | 169      | 22        | 12,435                | 169    | 22   |  |
| Ratio of means (r) $\equiv \widetilde{T}_{Q}$      | 10,153                | 205      | 20        | 5,160                 | 403    | 14   |  |
| Separate ratio (st) $\equiv \widetilde{T}_{Q}(st)$ | 4,980                 | 426      | 14        | 3,854                 | 682    | 12   |  |
| Combined ratio (st) $\equiv \widetilde{T}_{c}(st)$ | 6,775                 | 315      | 16        | 5,952                 | 372    | 15   |  |

<sup>\*</sup>R.E. is relative efficiency with the variance of  $\overline{T}_{X}$  as numerator.

Table 3b

VARIANCE OF ESTIMATOR AND RE LATIVE EFFICIENCY OF ESTIMATES
FOR PALAY PRODUCTION.

BULACAN PROVINCE. JULY 1959 TO JUNE 1960

| Concomitant variable  |   |   |   |  |   |  |  |  |  |
|-----------------------|---|---|---|--|---|--|--|--|--|
|                       | Number o  |   | Hectarage   |  |   |  |  |  |  |
| Variance<br>(000,000) | R.E.%*  | cv %  | Variance<br>(000,000)   | R.E.%*   | cv %  |  |  |  |  |
| 538,744               | 100   | 32  | 538,744   | 100  | 32  |  |  |  |  |
| 369,087               | 146   | 26  | 369,087   | 146  | 26  |  |  |  |  |
| 44,037                | 1,223   | 9   | 31,639  | 1,702  | 8   |  |  |  |  |
| 26,939                | 2,000   | 7   | 8,078   | 6,669  | 4   |  |  |  |  |
| 33,767                | 1,595   | 8   | 30,840  | 1,747  | 8   |  |  |  |  |
|                       | (000,000)<br>538,744<br>369,087<br>44,037<br>26,939 | Variance (000,000)       R.E.%*         538,744       100         369,087       146         44,037       1,223         26,939       2,000 | (000,000) R.E.%* cv %  538,744 100 32  369,087 146 26  44,037 1,223 9  26,939 2,000 7 | Variance (000,000)         R.E.%*         cv %         Variance (000,000)           538,744         100         32         538,744           369,087         146         26         369,087           44,037         1,223         9         31,639           26,939         2,000         7         8,078 | Variance (000,000)         R.E.%*         cv %         Variance (000,000)         R.E.%*           538,744         100         32         538,744         100           369,087         146         26         369,087         146           44,037         1,223         9         31,639         1,702           26,939         2,000         7         8,078         6,669 |  |  |  |  |

<sup>\*</sup>R.E. is relative efficiency with the variance of  $\overline{T}_{_{\mbox{\scriptsize X}}}$  as numerator.

|   | Concomitant variable  |          |      |                       |        |      |  |  |  |  |
|---|-----------------------|----------|------|-----------------------|--------|------|--|--|--|--|
|   |                       | Number o |      | Hectarage             |        |      |  |  |  |  |
| Type of estimator                                     | Variance<br>(000,000) | R.E.%*   | ev % | Variance<br>(000,000) | R.E.%* | ev % |  |  |  |  |
| Simple random $= \overline{T}_{x}$ (X-only)           | 402,376               | 100      | 24   | 402,376               | 100    | 24   |  |  |  |  |
| Stratified (optimum) $\equiv \overline{T}_{\chi}(oa)$ | 141,383               | 285      | 15   | 141,383               | 285    | 15   |  |  |  |  |
| Ratio of means $(r) = \widetilde{T}_{Q}$              | 31,212                | 1,289    | 7 .  | 10,508                | 3,829  | 8    |  |  |  |  |
| Separate ratio (st) $= \widetilde{T}_{Q}(st)$         | 14,306                | 2,813    | 5    | 6,512                 | 6,179  | 3    |  |  |  |  |
| Combined ratio (st) $\equiv T_{c}(st)$                | 19,834                | 2,029    | 5    | 7,463                 | 5,392  | 3    |  |  |  |  |

<sup>\*</sup>R.E. is relative efficiency with the variance of  $\overline{T}_{X}$  as numerator.

Table 3d

VARIANCE OF ESTIMATOR AND RELATIVE EFFICIENCY OF ESTIMATES
FOR PALAY PRODUCTION.

TARLAC PROVINCE. JULY 1959 TO JUNE 1960.

| •   |                       |          | Concomita | nt variable           |           |      |
|---|-----------------------|----------|-----------|-----------------------|-----------|------|
| •   |                       | Number o | f farms   |                       | Hectarage |      |
| Type of estimator   | Variance<br>(000,000) | R.E.%*   | cv %      | Variance<br>(000,000) | R.E.%*    | cv % |
| Stratified (optimum) $\equiv \overline{T}_{X}(oa)$ (X-only)     | 2,041,334             | 100      | 44        | 2,041,334             | 100       | 44   |
| Stratified (optimum) $= \overline{T}_{X}(oa)$                   | 532,098               | 384      | 22        | 532,098               | 384       | 22   |
| Ratio of means (r) $\equiv \widetilde{\mathrm{T}}_{\mathbf{Q}}$ | 760,322               | 268      | 27        | 229,080               | 891       | 15   |
| Separate ratio (st) $\equiv \tilde{T}_{Q}(st)$                  | 217,449               | 939      | 14        | 111,427               | 1,832     | 10   |
| Combined ratio (st) $\equiv \tilde{T}_{c}(st)$                  | 269                   | 758      | 16        | 146,600               | 1,392     | 12   |

\*R.E. is relative efficiency with the variance of  $\overline{T}_{\mathbf{x}}$  as numerator.

Table 3e

VARIANCE OF ESTIMATOR AND RELATIVE EFFICIENCY OF ESTIMATES

FOR PALAY PRODUCTION.

ZAMBALES PROVINCE. JULY 1959 TO JUNE 1960.

|  |                       |          | Concomita | nt variable           |        |      |  |
|--|-----------------------|----------|-----------|-----------------------|--------|------|--|
|  |                       | Number o |           | Hectarage             |        |      |  |
| Type of estimator                                      | Variance<br>(000,000) | R.E.%*   | cv %      | Variance<br>(000,000) | R.E.%* | cv % |  |
| Simple random $= \overline{T}_{x}$ (X-only)            | 66,334                | 100      | 41        | 66,334                | 100    | 41   |  |
| Stratified (optimum) = $\overline{T}_{X}$ (oa)         | 20,557                | 323      | 23        | 20,557                | 323    | 23   |  |
| Ratio of means (r) $\equiv \widetilde{T}_{\mathbf{Q}}$ | 4,420                 | 1,500    | 11        | 3,891                 | 1,704  | 10   |  |
| Separate ratio (st) $\equiv \widetilde{T}_{Q}(st)$     | 1,399                 | 4,742    | 6         | 1,894                 | 3,502  | 7    |  |
| Combined ratio (st) $\equiv \widetilde{T}_{C}(st)$     | 3,373                 | 1,966    | 9         | 3,073                 | 2,158  | 9    |  |
|  |                       |          |           |                       |        |      |  |

<sup>\*</sup>R.E. is relative efficiency with the variance of  $T_{\chi}$  as numerator.

Hectarage appears to be a more efficient concomitant variable than number of farms reporting as indicated by the lower variance or by the higher R.E. Tables (3a to 3e). The relatively high correlations between  $(X_{ij})$  and  $(Z_{ij})$  and between  $(X_{ij})$  and  $(Y_{ij})$  are responsible for the considerable gain in the statistical precision of the ratio estimators. The correlation coefficients by strata and by province are given in Table 4. Note that in addition to the five provinces of Abra, Bulacan, Pampanga, Tarlac, and Zambales, Table 4 gives the results for 15 other provinces.

#### III. Discussion and Recommendation

To be of maximum use as a sampling frame, the results of the Philippine 1960 Agricultural Census, must be tabulated at least at the barrio level. With stratification by size and by category (a to e), the variability among barrios as primary sampling units (PUS's) will be relatively lower than with the municipalities as PSU's. The application of stratification with the five categories (a to e) as strata resulted in a gain of statistical precision of 46 percent for Bulacan and 284 percent for Tarlac. In addition, this type of stratification will enable us to derive precise estimates of palay production and other charateristics for each province by each category, namely: (a) First crop, irrigated; (b) first crop, not irrigated; (c) second crop, irrigated; (d) second crop, not irrigated; and (e) kaingin and upland. These estimates will be useful in the preparation and evaluation of agricultural development efforts at the provincial level.

The barrios may arranged into paper strata in each of the five categories (a to e). After application of the paper strata, the product

## $N_iS_i$

will be approximately constant for all strata (i), where  $N_i$  is the number of farms and  $S_i$  is the standard deviation of palay production. As shown by the author (4), this condition

Table 4

CORRELATION COEFFICIENT BETWEEN PALAY PRODUCTION  $(X_{ij})$  IN CAVANS, AND NUMBER OF FARMS REPORTING  $(Z_{ij})$  AND HECTARAGE  $(Y_{ij})$  BY STRATA AND BY PROVINCE.

|                    |        |      | ρ̂(X | ., Z | <sub>ij</sub> ) |          | $\hat{\rho}(X_{ij}, Y_{ij})$ |      |       |      |      |              |
|--------------------|--------|------|------|------|-----------------|----------|------------------------------|------|-------|------|------|--------------|
| Province           | Strata |      |      |      |                 | Whole    |                              | S    | tra   | t a  |      | Whole        |
|                    | (a)    | (b)  | (c)  | (d)  | (e)             | province | (a)                          | (b)  | (c)   | (d)  | (e)  | province     |
| Abra               | 0.78   | 0.87 | 0.82 | 0.85 | 0.59            | 0.90     | 0.91                         | 0.94 | 0.91  | 0.89 | 0.26 | 0.87         |
| Bulacan            | .96    | .97  | .98  | .99  | .93             | .96      | .99                          | .98  | .99   | .99  | .98  | .97          |
| Pampanga           | .95    | .95  | .95  | .99  | .95             | . 95     | .97                          | .99  | .98   | .99  | .98  | .98          |
| Tarlac             | .75    | .90  | .95  | . 85 | .94             | .81      | .87                          | .98  | .97   | .99  | .99  | . <b>9</b> 5 |
| Zambales           | .99    | .93  | .99  | .98  | .96             | .97      | . 99                         | .93  | . 95  | . 93 | .94  | . 97         |
| Aklan              | . 95   | .90  | . 95 | . 91 | .90             | . 90     | .96                          | .91  | . 97  | .98  | .95  | . 96         |
| Albay              | .88    | .93  | .81  | .92  | .94             | .74      | .95                          | .99  | .91   | .99  | .99  | . 92         |
| Bataan             | .77    | .95  | .79  | .92  | .92             | .82      | .92                          | .99  | .92   | .99  | .98  | .94          |
| Cagayan            | .87    | . 82 | .96  | .97  | .91             | .83      | . 95                         | . 97 | .99   | .96  | .96  | .97          |
| Camarines Norte    | .95    | .98  | .95  | .94  | . 99            | .71      | .99                          | .98  | .98   | .98  | .99  | .93          |
| Catanduanes        | .77    | . 95 | .80  | .97  | .94             | .82      | . 82                         | .95  | .81   | .92  | .96  | .87          |
| Ilocos Norte       | .92    | .90  | .99  | .98  | .58             | . 89     | .88                          | .91  | .97   | .99  | .99  | . 92         |
| Misamis Occidental | .94    | .73  | .91  | . 56 | .92             | .85      | . 99                         | .91  | . 93  | .96  | .88  | .81          |
| Misamis Oriental   | .93    | .98  | .94  | .97  | .95             | . 89     | .99                          | .97  | . 99  | .97  | . 99 | .98          |
| Nueva Ecija        | .99    | .94  | .97  | .98  | .76             | .83      | .99                          | .99  | .99   | . 99 | . 88 | . 84         |
| Nuova Viscava      | .95    | .97  | .91  | .74  | .98             | .93      | .99                          | .97  | .9C   | . 95 | .98  | . 97         |
| Preidental Mindoro | .91    | .96  | .99* | .77  | .84             | .94      | .96                          | .99  | .99*  |      | . 97 | . <b>9</b> 9 |
| Romblon            | .95    | .97  | .93  | . 58 | .99             | .90      | .95                          | .99  | .99   | .97  | . 99 | . 95         |
| Foresogen          | .77    | .95  | .78  | .98  | .97             | . 80     | .96                          | 95   | 96    | .97  | .97  | . 93         |
| Surigao del Sur    | .99    | .95  | **   | . 43 | .98             | .92      | .99                          | .98  | T1 T7 | .96  | . 99 | . 98         |

<sup>\*</sup>Contains three pairs of observations.

will indicate that the technique of equal take is as precise as stratified optimum sampling. Also, the administrative requirements of the survey become more simple with equal take. Thus, with equal take, statistical and administrative efficiencies are improved. From the census frame, each sample barrio is drawn from a given stratum with replacment and with probability proportional to size (pps) of production. estimates are adjusted with the use of ratio estimators. The concomitant variables in the ratio estimators will be the number of farms reporting (Zii) or the hectarage (Yii) which are obtained from independent sources. As shown in this paper, the correlation between production  $(X_{ii})$  and number of farms reporting (Z<sub>ij</sub>) is about 0.87 while the correlation between production  $(X_{ij})$  and hectarage  $(Y_{ij})$  averaged about 0.94. High levels of correlation exist in the 20 provinces where census results have been released by the Bureau of the Census and Statistics. Thus, we expect considerable gain in statistical efficiency in the use of ratio estimators in efficiency in the use of ratio estimators in each of these provinces.

As the Philippine 1960 census was a sample census, then the statistical findings presented in this paper can be used to improve the results of the 1960 census. These findings also will be incorporated into the estimation procedure of the current Philippine palay survey of the Bureau of Agricultural Economics, Department of Agriculture and Natural Resources.

#### IV. Review of Literature

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# ESTIMATION OF PALAY PRODUCTION WITH THE 1960 AGRICULTURAL CENSUS AS THE SAMPLING FRAME

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